

AB Calculus Quiz 12 vA
 FTC & Properties of Integrals
 Dr. Wisniewski Spring 2020

23 total pts

Name Solution Daihatsü Period _____

Instructions: Work each of the following problems showing as much work as possible. A calculator is not permitted on this quiz.

1. (6 Pts) Given $\int_{-3}^2 f(x) dx = 7$, $\int_{-3}^2 g(x) dx = -4$ and $\int_{-3}^5 f(x) dx = 15$, find

a. $\int_{-3}^2 2g(x) dx$
 $= 2 \int_{-3}^2 g(x) dx = (2)(-4) = \boxed{-8}$

d. $\int_{-3}^2 [f(x) + 5] dx = \int_{-3}^2 f(x) dx + \int_{-3}^2 5 dx$
 $7 + 5 \cdot 5 = \boxed{32}$

b. $\int_{-3}^2 [f(x) - g(x)] dx$
 $\int_{-3}^2 f(x) dx - \int_{-3}^2 g(x) dx =$
 $7 - (-4) = \boxed{11}$

e. $\int_2^5 f(x) dx = \int_{-3}^5 f(x) dx - \int_{-3}^2 f(x) dx$
 $15 - 7 = \boxed{8}$

c. $\int_2^{-3} g(x) dx = - \int_{-3}^2 g(x) dx$
 $= -(-4) = \boxed{4}$

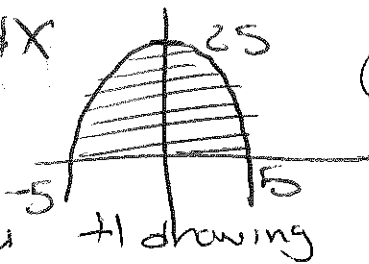
f. $\int_1^1 f(x) dx = \boxed{0}$

2. (3 Pts) Find the area of the region enclosed by the graph of $y = 25 - x^2$ and the x -axis. Construct a sketch of the region and shade the enclosed area.

$A = \int_{-5}^5 (25 - x^2) dx = 2 \int_0^5 (25 - x^2) dx$

$= 2 \left[25x - \frac{x^3}{3} \right]_0^5$ +1 for integration
 +1 for execution answer

$= 2 \left[25 \cdot 5 - \frac{125}{3} \right] = 2 \left[125 - \frac{125}{3} \right] = 2 \left[\frac{375 - 125}{3} \right] = \frac{2}{3} (250) = \boxed{\frac{500}{3}}$



$\frac{500}{3}$ if they think it's a circle.

3 pts

3. (12 Pts) Evaluate each of the following integrals.


$$\begin{aligned} 3x+2 &= 0 \\ 3x &= -2 \\ x &= -2/3 \end{aligned}$$

a. $\int_{-2}^2 4x^3 dx = 4 \int_{-2}^2 x^3 dx$
 $\left. \frac{4x^4}{4} \right|_{-2}^2 = 0$ (odd)

d. $\int_{-2}^1 |3x+2| dx = \int_{-2}^{-2/3} -(3x+2) dx + \int_{-2/3}^1 (3x+2) dx$

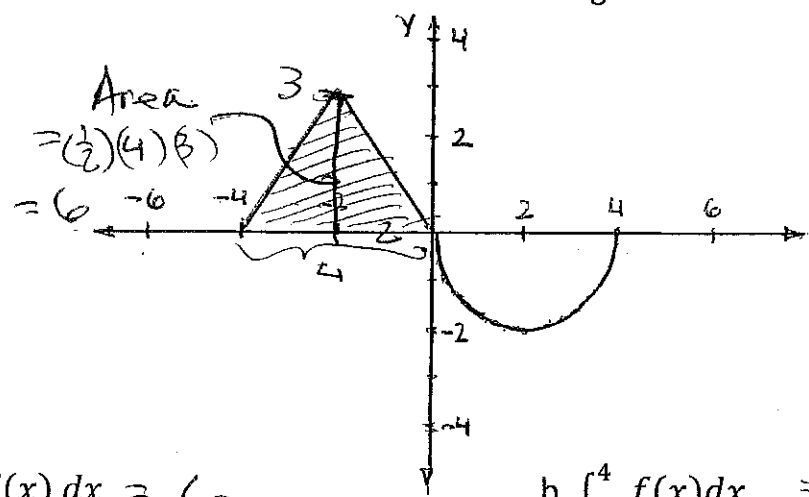
b. $\int \frac{x^2-2x+3}{x} dx$
 $\int (x-2+\frac{3}{x}) dx$ $\therefore \int$ fast no const.
 $= \left[\frac{x^2}{2} - 2x + 3 \ln|x| + C \right]$

e. $\int_{-3}^3 x^{-2} dx$
 FTC DNA
 $\frac{1}{x} \rightarrow$ discontinuous @ $x=0$
 $\left. \frac{3x^2}{2} + 2x \right|_{-3}^3 + \left. \frac{3x^2}{2} + 2x \right|_{-2/3}^{-2/3}$
 6.833 $4/6$ $6.9/6$

c. $\int_{-\pi/2}^{\pi/2} \cos x dx$

 $= 2 \int_0^{\pi/2} \cos x dx = 2 [\sin x]_0^{\pi/2}$
 $= 2(\sin \pi/2 - \sin 0)$
 $2 \cdot 1 = 2$

f. $\int \sec \theta \tan \theta d\theta$
 $= \boxed{\sec \theta + C}$

4. (2 Pts) The graph of the function $y = f(x)$ is given below. The graph is made up of a triangle and a semi-circle. Evaluate the two integrals.



a. $\int_{-4}^0 f(x) dx = 6$

b. $\int_{-2}^4 f(x) dx = 3 - \pi \cdot \frac{2^2}{2}$
 $\boxed{3 - 2\pi}$
 9/4 pts